

For a venturi meter with a manometer, the volumetric flow rate \dot{V} is calculated with:

$$\dot{V} = C_f A_t \sqrt{2 g h \left(\frac{\rho_m}{\rho} - 1 \right)} \quad (1)$$

where C_f is the meter's flow coefficient, A_t is the cross-section area at the throat, ρ_m is the density of the manometer fluid, and ρ is the density of the pipe fluid. This equation can be re-written as:

$$\dot{V} = C_f A_t \sqrt{2 g \left(\frac{\rho_m}{\rho} - 1 \right)} \cdot \sqrt{h} \quad (2)$$

The fact that $\dot{V} = 400$ gpm for $h = 8$ in , can be used with equation (2) to determine that:

$$C_f A_t \sqrt{2 g \left(\frac{\rho_m}{\rho} - 1 \right)} = 141.42 \frac{\text{gpm}}{\text{in}^{1/2}} \quad (3)$$

In other words, we recognize that the left side of equation (3) is a constant and its numerical value is the same if only the height h changes. Therefore, equation (2) can be re-written as:

$$\dot{V} = \left[141.42 \frac{\text{gpm}}{\text{in}^{1/2}} \right] \sqrt{h}$$

which yields $\dot{V} = 283$ gpm for $h = 4$ in . The average fluid velocity in the pipe $V = \dot{V} / A$ is then

$$V = \frac{283 \frac{\text{gal}}{\text{min}} \left| \frac{1 \text{ ft}^3}{7.48 \text{ gal}} \right|}{\pi \left(\frac{2.067 \text{ in}}{2} \right)^2 \left| \frac{1 \text{ ft}}{12 \text{ in}} \right|^2} = 1.623 \frac{\text{ft}}{\text{min}}$$

The correct answer is (D)

